

M7

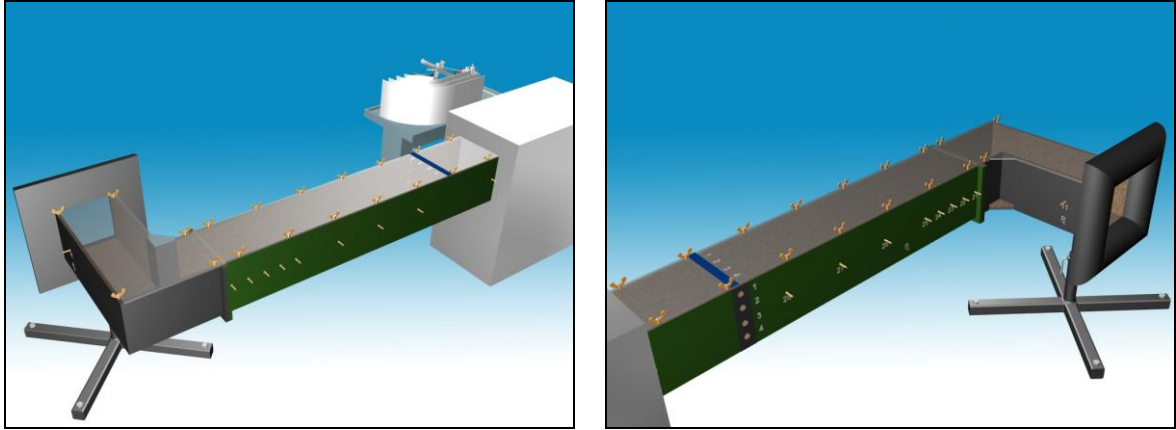
## INVESTIGATION OF THE LOSS COEFFICIENT AND THE FLOW FIELD OF AN ELBOW

### 1. The aim and practical aspects of the measurement

In pipelines the direction of the flow is usually changed with elbows, i.e. with curved tubes. The change in the direction causes losses, for the reduction of which many methods have been developed. The aim of this measurement is the investigation of the reduction of the losses in an elbow using different geometrical elements. The goal is to find the method providing the best solution.

### 2. Description of the measurement

The elbow, which is being investigated, has a cross-section of  $150 \times 150$  mm. A fan which is attached to the end of the duct sucks the air through the system. The air enters the duct upstream of the elbow through a conical inlet orifice. It is assumed that the inlet has minimal losses, and that the air comes from the undisturbed environment. In this way a uniform flow can be realized upstream of the elbow. Downstream of the elbow, static pressure taps can be found along the length of the longer section of the duct. We can examine the flow visually through the plexiglas top of the measurement set-up using pins with long fluffy threads attached to them.



### 2.1 Volume flow rate, average velocity

The pressure difference between the pressure tap which can be found right after the inlet to the duct and the ambient pressure,  $\Delta p_{meas}$  gives a good approximation of the dynamic pressure experienced in the duct. The volume flow rate calculated as:

$$q_v = k \cdot A \cdot \sqrt{\frac{2}{\rho} \cdot \Delta p_{meas}} = k \cdot a^2 \cdot \sqrt{\frac{2}{\rho} \cdot \Delta p_{meas}}$$

where  $\rho$  is the density of the fluid, and  $k$  is the correction factor in order to account for the wall friction and the inlet losses.

The  $\bar{v}$  average velocity can be expressed as:

$$\bar{v} = \frac{q_v}{A} = k \cdot \sqrt{\frac{2}{\rho} \cdot \Delta p_{meas}}$$

The  $k$  correction factor can be determined with the average velocity.

The average velocity can be determined by using a Prandtl tube, otherwise known as a Pitot-static tube, and the point to point measurement technique. In this case the measurements should be made upstream of the bend in  $2 \times 2 = 4$  points. Note though, that the  $\bar{v}$  can change with the introduction of the different elements into the flow (the loss coefficient can change as well).

The average velocity determined by the point to point measurement technique:

$$\bar{v} = \frac{\sum_{i=1}^4 v_i}{4} = \frac{\sum_{i=1}^4 \sqrt{\frac{2 \cdot p_{dyn,i}}{\rho}}}{4}$$

where  $p_{dyn,i}$  is the dynamic pressure measured at the  $i$ -th point.

The  $k$  correction factor:

$$k = \frac{\sum_{i=1}^4 \sqrt{\frac{2 \cdot p_{\text{dyn},i}}{\rho}}}{\sqrt{\frac{2 \cdot \Delta p_{\text{meas}}}{\rho}}} = \frac{\sum_{i=1}^4 \sqrt{p_{\text{dyn},i}}}{4 \cdot \sqrt{\Delta p_{\text{meas}}}}$$

Determining the correction factor should be the first step during the measurement. Knowing the  $k$  correction factor, which is constant, the use of the Prandtl tube is no longer necessary. The volume flow rate and average velocity can now be calculated using the  $\Delta p_{\text{meas}}$ .

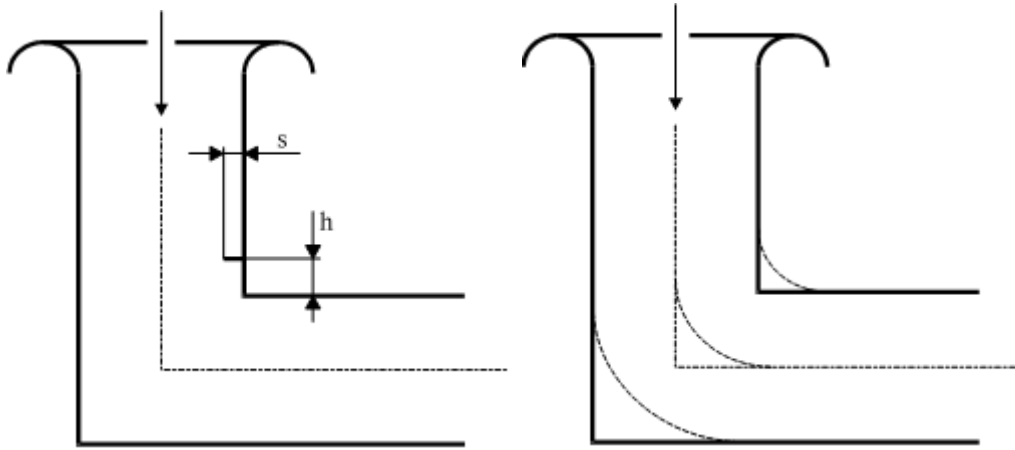
## 2.2 Loss coefficient

The quality of the elbow is determined by its pressure loss, using the  $\xi_e$  loss coefficient. The loss coefficient can be expressed as the difference between the total pressure upstream ( $p_{t,b}$ ) of the bend and the total pressure downstream ( $p_{t,a}$ ) of it divided by the dynamic pressure ( $p_{\text{dyn}}$ ).

$$\xi_e = \frac{p_{t,b} - p_{t,a}}{\frac{\rho}{2} v^2}$$

The value of the loss coefficient is influenced by the flow field, with an especially large influence coming from the size of the separation bubbles. In order to guide the air through the bend of the elbow an overpressure is required at the inlet of the duct in order to overcome the secondary losses from the secondary flows and the separation bubbles. If the extent of the secondary losses can be reduced, then the  $\xi_e$  can be reduced. This can be achieved by adding different elements into the elbow (Fig. 1) by:

- rounding the inner and outer corners of the elbow with elements having different radius, or by using a 45° plate instead of the sharp corner. Other elements can also be added in the middle of the elbow cross section, which are parallel with the curved walls of the elbow.
- placing different elements (L shaped elements) into the flow, which block the flow in certain areas of the duct and therefore give control over the positioning, size and shape of the separation bubbles. In this way smaller separation zones, having a certain amount of pressure loss associated with them, can be formed, which inhibit the forming of the larger separation zones, and therefore reduce the losses in the duct. In this case the proper size and positioning of the L shaped elements needs to be determined. The different elements can be attached to the wall of the duct both upstream and downstream of the elbow on either side of the channel.



*Fig. 1.: Different possibilities for manipulating the flow in the elbow.*

### 2.3 Flow visualization

The measuring apparatus can be used for flow visualization as well. In order to do this either a rod with a long fluffy thread attached to its end can be used, or a number of pins having the same type of threads attached to their ends can be pinned into the cork bottom of the measurement apparatus. In this case, the second possibility will be used. It is advised that a record of the flow fields be kept for the different set-ups, so that these can be included in the laboratory report.

## 3. Description of the measurement

### 3.1 Loss coefficient

In order to calculate the loss coefficient, we need to calculate the total pressure difference:  $(p_{t,b} - p_{t,a})$ . On the other hand, since the cross-section of the duct is the same before as well as after the bend, the dynamic pressure is going to be the same in both cross-sections because of continuity.

$$p_{t,b} - p_{t,a} = (p_{st,b} + p_{dyn,b}) - (p_{st,a} + p_{dyn,a}) = (p_{st,b} + \frac{\rho}{2} \bar{v}^2) - (p_{st,a} + \frac{\rho}{2} \bar{v}^2) = p_{st,b} - p_{st,a}$$

The dynamic pressure of the average velocity can be determined by using the  $k$  and  $\Delta p_{meas}$ .

$$\frac{\rho}{2} \bar{v}^2 = k^2 \cdot \Delta p_{meas}$$

Therefore the equation for the loss coefficient can be reduced in the following matter

$$\zeta_k = \frac{p_{st,b} - p_{st,a}}{k^2 \cdot \Delta p_{meas}}$$

During the measurement, we can directly measure the pressure difference by connecting the one end of the manometer to the tap which is upstream of the bend and the other one to the taps which are downstream of the bend.

$p_{st,b}$ : The upstream static pressure tap is obvious in the measurement set-up. Here the upstream effect of the elbow onto the flow can be neglected.

$p_{st,a}$ : In choosing the downstream measurement point, the main question is, how far does the disturbing effect of the elbow influence the measurement, and therefore which

measurement point should be used? After the bend in the duct, the two sidewalls have 8-10 taps placed at a certain interval, which can be used for measuring the static pressure. In examining the streamlines and the pressure reading results, it can be found, where the flow separation on the wall of the duct reattaches (using the flags), which should coincide with the cross-section where the pressure readings on both sides of the duct are approximately the same, due to the almost parallel streamlines. It should be noted though, that since the velocity profiles at this cross-section are not yet entirely symmetric, we are looking for the cross-section where the measured static pressure does not increase further. Here it can be said that the flow has reattached to the wall of the duct and that the velocity profile is once again symmetric. This is the static pressure which should be considered as the downstream value of the static pressure, and with which the loss coefficient of the elbow should be calculated.

/The two sets of pressure taps which are closest to the fan do not give accurate readings due to the inlet to the fan, and therefore should not be considered during the measurement./

The  $\xi_e$  needs to be examined for different set-ups, with the goal being the attainment of a  $\xi_{e,\min}$  value.

### 3.2 Power loss

The pressure loss due to the elbow has to be covered by power. Because of the loss the used electric power is more than necessary. The power loss can be determined:

$$P_{\text{loss}} = q_v \cdot (p_{t,b} - p_{t,a}) = k \cdot A \cdot \sqrt{\frac{2}{\rho} \cdot \Delta p_{\text{meas}}} \cdot (p_{st,b} - p_{st,a})$$

### 3.3 Error calculation

The absolute error calculation:

$$\delta R = \sqrt{\sum_{i=1}^n \left( \delta X_i \cdot \frac{\partial R}{\partial X_i} \right)^2}$$

where  $X_i$  is the measured amount and  $\delta X_i$  is the measurement error associated with it.

The relative error calculation:

$$\frac{\delta R}{R} = ?$$

In the laboratory report, both the relative and absolute errors need to be given for the loss coefficient and the power loss. The measurement errors associated with the loss coefficient:

$$X_1 = p_{st,b} - p_{st,a}$$

$$\text{Error of the digital manometer: } \delta p_{dig} = 2Pa$$

$$X_2 = \Delta p_{meas}$$

$$\text{Error of the digital manometer: } \delta p_{dig} = 2Pa$$

The measurement errors associated with the power loss:

$$X_1 = p_{st,b} - p_{st,a}$$

$$\text{Error of the digital manometer: } \delta p_{dig} = 2Pa$$

$$X_2 = \Delta p_{\text{meas}}$$

Error of the digital manometer:  $\delta p_{\text{dig}} = 2 \text{ Pa}$

$$X_3 = T_o$$

Error of the temperature measurement:  $\delta T_o = 1 \text{ K}$

$$X_4 = p_o$$

Error of the barometer:  $\delta p_o = 100 \text{ Pa}$

#### 5. The measurement assignments:

- Measure the ambient pressure and temperature
- Calibrate the digital manometer
- Calibrate the inlet
- Measure the pressure taps' positions
- Measure  $\Delta p_{\text{mért}}$  to calculate the volume flow rate
- The pressure distribution after the elbow at both sides of the channel
- Flow visualization to the different elements

#### 4. The report should contain the following:

- Pitot-static tube measurement data, and the value for the average velocity and calibration constant.
- The calibration of the digital manometer should be presented.
- A table containing the static pressure values, the pressure distribution along the wall of the duct, as a function of the length (x[mm]).( The positions of the different pressure taps should be measured!) A diagram with the two separate pressure distributions on the two sides of the duct, which should be made for every set-up.
- Photos of the different flow visualization results for the different set-ups.
- It needs to be determined where the flow reattaches to the wall of the duct, and therefore, where the velocity profile is symmetric. The loss coefficient for the particular set-up needs to be calculated at this point.
- Results should be presented for all the examined cases in a similar manner.
- Error calculation.
- The different set-ups should be compared, with the results being given in a tabular or graphical manner, pointing out the most advantageous and the disadvantageous set-ups. Do not forget to examine the basic empty duct with the 90° elbow, which is the reference duct for the measurements. By comparing the loss coefficients of the different set-ups to these, we can arrive at different conclusions for our results.
- There should be an individual evaluation made of all the different results.
- Error calculations should be made for the measurement results of the loss coefficient and power loss, based on what is assigned.
- Summary.

***Remember that during the labs:***

- Before turning any measurement device on or in general during the lab, make sure that safe working conditions are ensured. The other participants have to be warned of the starting of the machines and of any changes that could endanger the members of the lab.
- The atmospheric pressure and room temperature should be recorded before and after every measurement.
- The measurement units and other important factors (e.g. data sampling frequency, date of calibration) of every recorded value of the applied measurement devices should be recorded.
- Type and construction number of the applied measuring instrument should be included in the final report.
- Checking and harmonizing of the units of the recorded values with those used in further calculations.
- The digital manometer must be calibrated.
- The measurement ports of the pressure meter should be carefully connected to the correct pressure ports of the instrument.
- If inlet or outlet tubes are to be assembled with fans, connections should be airtight as escaping/entering air can significantly modify the measurement results.
- The students should consult with their instructor before submitting the report.

**Bibliography:**

Lajos Tamás: Az áramlástan alapjai, Budapest 2008, (10. fejezet Hidraulika)